

NH - 67, Karur - Trichy Highways, Puliyur C.F, 639 114 Karur District

## **MA8491-NUMERICAL METHODS**

## **UNIT-III- Numerical Differentiation and Integration**

1. The below mentioned formula is suitable to find out

$$\int_{x_0}^{x_n} y \, dx = nh[y_0 + \frac{n}{2}\Delta y_0 + \frac{n(2n-3)}{12}\Delta^2 y_0 + \frac{n(n-2)^2}{24}\Delta^3 y_0 + \cdots]$$

- A. Simpson's 1/3 rule
- B. Simpson's 3/8 rule
- C. Trapezoidal rule
- D. Newton Cote's formula

Answer: (D)

2. The below mentioned formula is suitable to find out

$$\int_{x_0}^{x_n} y \, dx = \frac{h}{2} \left[ (y_0 + y_n) + 2(y_1 + y_2 + y_3 + \dots + y_{n-1}) \right]$$

- A. Simpson's 1/3 rule
- B. Simpson's 3/8 rule
- C. Trapezoidal rule
- D. Newton Cote's formula

Answer: (C)

3. The below mentioned formula is suitable to find out

$$\int_{x_0}^{x_n} y \, dx = \frac{h}{3} \left[ (y_0 + y_n) + 4(y_1 + y_3 + y_5 + \dots) + 2(y_2 + y_4 + y_6 + \dots) \right]$$
is the formula of

## A. Simpson's 1/3 rule

- B. Simpson's 3/8 rule
- C. Trapezoidal rule
- D. Newton Cote's formula

Answer: (A)

4. The below mentioned formula is suitable to find out

$$\int_{x_0}^{x_n} y \, dx = \frac{3h}{8} [(y_0 + y_n) + 3(y_1 + y_2 + y_4 + y_5 + \dots) + 2(y_3 + y_6 + y_9 + \dots)]$$

- A. Simpson's 1/3 rule
- B. Simpson's 3/8 rule
- C. Trapezoidal rule
- D. Newton Cote's formula

- 5. Which formula is called closed formula?
- A. Simpson's rule
- B. Trapezoidal

Answer: (A)

- 6. What is the condition to apply Simpson's  $\frac{1}{3}$  rule for integration?
- A. The interval of integration must be divided into an even number of sub-intervals.
- B. The interval of integration must be divided into an odd number of sub-intervals.
- C. The interval of integration must be divided into 3 sub-intervals
- D. The interval of integration must be divided into 6 sub-intervals Answer: (A)
- 7. In Simpson's  $\frac{3}{R}$  rule for integration the interval of integration must be divided into how many sub intervals?
- A. 2
- B. **3**
- C. 4
- D. 5

Answer: (B)

- 8. In Simpson's 3/8 rule the interval of integration is divided into
- A. The interval of integration must be divided into an even number of sub-intervals.
- B. The interval of integration must be divided into an odd number of sub-intervals.
- C. The interval of integration must be divided into multiple of 3 sub-intervals
- D. The interval of integration must be divided into 10 sub-intervals

Answer: (C)

- 9. What is the order of error in Trapezoidal rule?
- **A.**  $h^2$
- B.  $h^{3}$
- C.  $h^4$
- D.  $h^{5}$

- 10. What is the order of error in Simpson's  $\frac{1}{3}$  rule (or) Simpson's rule?
- A.  $h^2$
- B.  $h^{3}$
- C. *h*<sup>4</sup>
- D.  $h^{5}$

Answer: (C)

- 11. What is the order of error in Simpson's  $\frac{3}{8}$  rule?
- A.  $h^2$
- B.  $h^{3}$
- C. *h*<sup>4</sup>
- **D.**  $h^{5}$

Answer: (D)

12. What is the error in Trapezoidal rule?

A. 
$$E = \frac{(b-a)}{12}h^2y''(x)$$

B. 
$$E = -\frac{(b-a)}{14}h^2y''(x)$$

C. 
$$E = -\frac{(a-b)}{12}h^2y''(x)$$

**D.** 
$$E = -\frac{(b-a)}{12}h^2y''(x)$$

Answer: (D)

13. What is the error in Simpson's  $\frac{1}{3}$  rule (or) Simpson's rule?

A. 
$$E = \frac{(b-a)}{180} h^4 y^{iv}(x)$$

B. 
$$E = -\frac{(a-b)}{150}h^4y^{i\nu}(x)$$

C. 
$$E = -\frac{(b-a)}{180}h^4y^{iv}(x)$$

D. 
$$E = \frac{(b-a)}{150} h^4 y^{iv}(x)$$

Answer: (C)

14. What is the error in Simpson's  $\frac{3}{8}$  rule?

**A.** 
$$E = -\frac{3(b-a)}{80}h^5y^{iv}(x)$$

B. 
$$E = \frac{3(b-a)}{80}h^5y^{iv}(x)$$

C. 
$$E = -\frac{3(b-a)}{50}h^5y^{iv}(x)$$

D. 
$$E = -\frac{3(b-a)}{50}h^4y^{iv}(x)$$

- 15. If  $I_1 = 0.775$  and  $I_2 = 0.7430$  with h = 0.5 and h = 0.25, find I using Romberg's method.
- A. **0.7802**
- B. 0.7602
- C. 0.7805
- D. 0.7702
- Answer: (A)
- 16. Gaussian 2-point quadrature formula for integration is

$$\mathbf{A.} \int_{-1}^{1} f(t)dt = f\left(-\frac{1}{\sqrt{3}}\right) + f\left(\frac{1}{\sqrt{3}}\right)$$

B. 
$$\int_{-1}^{1} f(t)dt = f\left(-\frac{1}{\sqrt{5}}\right) + f\left(\frac{1}{\sqrt{5}}\right)$$

C. 
$$\int_{-1}^{1} f(t)dt = f\left(-\frac{1}{\sqrt{3}}\right) + f\left(\frac{1}{\sqrt{5}}\right)$$

D. 
$$\int_{-1}^{1} f(t)dt = f\left(-\frac{1}{\sqrt{5}}\right) + f\left(\frac{1}{\sqrt{3}}\right)$$

Answer: (A)

- 17. Trapezoidal formula is also known as \_\_\_\_\_
- A. Simpson's rule
- B. Co-ordinate method
- C. Prismoidal method
- D. Average end area method

Answer: (D)

- 18. The value obtained from Simpson's rule depends on the nature of the curve.
- A. True
- B. False

- 19. In which of the following cases, Simpson's rule is adopted?
- A. When straights are perpendicular
- B. When straights are parallel
- C. When straights form curves
- D. When straights form parabolic arcs

Answer: (B)

- 20. Which of the following shapes is generally preferred in case of application of Simpson's rule?
- A. Square
- B. Triangle
- C. Trapezoid
- D. Rectangle

Answer: (C)

- 21 Which of the following can the Simpson's rule possess?
- A. Negatives
- **B.** Accuracy
- C. Positives
- D. Zero error

Answer: (B)

- 22. Simpsons rule will give exact result, if the entire curve y=f(x) is a
- A. hyperbola
- B. parabola
- C. ellipse
- D. cone

Answer: (B)

- 23. By Gaussian two point formula  $\int_{-1}^{1} (3x^2 + 5x^4) dx =$
- A. 3.311
- B. 3.211
- C. 3.112
- D. 3.213

Answer: (C)

24. If the range is not (-1,1), then what is the idea to solve the Gaussian quadrature problem.

**A.** 
$$x = \frac{b-a}{2}z + \frac{b+a}{2}$$

B. 
$$x = \frac{b+a}{2}z + \frac{b-a}{2}$$

C. 
$$x = \frac{b+a}{2} + \frac{b-a}{2}$$

D. 
$$x = \frac{b+a}{2}z - \frac{b-a}{2}$$

- 25. In Romberg's method which formula is used
- A. Simpson's 1/3 rule
- B. Simpson's 3/8 rule
- C. Trapezoidal rule
- D. Newton Cote's formula

Answer: (C)